Abstract. The purpose of this paper is to present modern tennis science to a wider scientific audience. A biomechanical analysis of tennis shots and the corresponding racket/ball dynamics is presented together with its analogy with handball throws. The main difference between these two sport games is in the tennis racket (as an additional body segment with its inertial and elastic characteristics). This presents anatomical, physiological and biomechanical analysis of the tennis serve, forehand and backhand, as well as a 3D Newton-Euler dynamical analysis of the tennis racket motion during these shots. In the future, numerical simulations will necessarily support similar analysis, together with the racket stress-strain elasticity analysis, as well as experimental measurement based on inertial sensors (accelerometers and gyroscopes, embedded in the frame of a racket) for tracking velocities and accelerations of a player’s movements in the tennis serve, forehand and backhand.

Key words: tennis shots, handball throws, biomechanical analysis, Newton-Euler dynamics, vestibular and artificial sensors
istics of tennis balls. Subsequently, Cross (2000) showed that, for impacts between bod-
ies, $e$ depends on the stiffness of each body. As a result, during impacts against a "rigid" 
surface, almost all of the energy dissipation occurs in the tennis ball.

On the other hand, the main difference between tennis and other ball games is not in 
the ball itself, but rather in the tennis racket. The active racket surface has different points 
(Figure 1), most notably the "Sweet spot" (Brody, 1981), which are effectively used by 
experienced players to obtain the optimal ball trajectory.

![Figure 1](image)

Ducher et al. (2005) studied bone geometry in response to long-term tennis playing 
and its relationship with muscle volume. Their quantitative magnetic resonance imaging 
study showed that the greater bone mineral content (BMC) induced by long-term tennis 
playing at the dominant radius was associated to a marked increase in bone size and a 
slight improvement in volumetric BMD, thereby improving bone strength. In addition to 
the muscle contractions, other mechanical stimuli seemed to exert a direct effect on bone 
tissue, contributing to the specific bone response to tennis playing.

Wright and Jackson (2007) used fMRI techniques to study brain regions concerned 
with perceptual skills in tennis. They found that the task of judgment of serve direction 
produced two different patterns of response: activations in the MT/MST and STS areas in 
the posterior part of the temporal lobe concerned with primarily the analysis of motion 
and body actions, and activations in the parietal and frontal cortex associated specifically 
with the task of identification of direction of serve.

Recently, Girard et al. (2008) studied neuromuscular fatigue in tennis. The time 
course of alteration in neuromuscular function of the knee extensor muscles was charac-
terized during a prolonged intermittent exercise. Central activation failure and alterations 
in excitation–contraction coupling were identified as probable mechanisms contributing 
to the moderate impairment of the neuromuscular function during prolonged tennis playing.

Recently, Bazzucchi et al. (2008) have found that tennis players, with a constant 
practice in controlling forces around the elbow joint, learn how to reduce co-activation of 
muscles involved in the control of this joint. This has been shown by the lower antagonist 
muscular activity of triceps brachii muscle during isokinetic elbow flexion found in ten-
nis players with respect to non-players.
There have been several physiological studies of tennis performance; see, e.g., (Bergeron et al., 1991). Recently, Reid and Schneiker (2008) reviewed current research and practice of strength and conditioning in tennis. They have pointed out that virtually all professional tennis players are in continuous pursuit of enhanced performance. With the modern game becoming increasingly dynamic and tournament schedules no less demanding, the importance of physical fitness is well accepted. Indeed, most professional tennis players resource strength and conditioning specialists on a full- or part-time basis. As tennis play is characterized by intricate bio-energetics, planning specific strength and conditioning interventions represents a significant challenge for the specialist.

In the present paper we will present anatomy, physiology and biomechanics of tennis shots, accompanied by the Newton—Euler dynamics of the tennis racket.

Fig. 2. Three phases of tennis serve: preparation (with the 'toss'), jump and shot

2. TENNIS BIOMECHANICS

2.1. Descriptive Mechanics of Tennis Shots

In tennis, we transfer the energy from our body to the ball via a tennis racket to generate speed and spin of the ball. Energy can be either potential (stored energy) or kinetic energy (energy of movement). A specific type of potential energy is elastic energy (that is, the energy which causes, or is released by, the elastic distortion of a solid or a fluid). An example of elastic energy is the energy stored in a spring under tension. The human equivalent would be energy stored in muscles and their tendons under tension. On the other hand, kinetic energy specifically refers to the work required to accelerate the ball from a resting position to a desired velocity.

Let's examine how the body transfers the necessary energy to the ball in a tennis stroke. Here, we think of the body as a series, or a chain, of linkages connected to one another and affecting each other in a specific sequence. For example, the foot is a link, which is connected to the leg by the ankle joint, which is in turn connected to the thigh by the knee joint and so on. During the initiation of a forehand ground-stroke (Figure 3) the feet are oriented for either an open stance or close stance position. The shoulder and torso are turned approximately 45 degrees, which in turn causes a "coiling" of the abdomen and pelvis, which in turn produce a slight knee bend. With the current forehand the racket is held fairly high at about head level. In this position there exists a great deal of potential
energy, both in the form of gravity with the racket head up high and the form of elastic stored energy in the tensed muscles that are stretched in the coiled position (both internal and external abdominal obliques muscles, pectorals major, forearm muscles, hip girdle musculature, quadriceps femoris). This energy is released and sequence and there is an overlap in the sequence of linkages. As the racket starts to drop and begin an oval path (loop) the hips start to uncoil. The hips and knees begin to straighten. In sequence with the uncoiling of the hips the next event is the uncoiling of the torso and then the shoulders as the racket is brought forward to contact the ball. At the same time, the back leg is fully extended to powerfully drive the body up and forward. In fact, many professional players actually leave the ground during this point. At ball contact only medium grip pressure is required to guide and stabilize the racket. This is because the forward momentum will carry the racquet through the ball without much effort. After contact the shoulder and torso and hips naturally rotate towards the non-dominant side following the path of the racquet resulting in a stretch of the opposite side musculature which decelerates the racquet.

![Fig. 3. Two phases of a tennis forehand: preparation and shot](image)

Completely analogous is the biomechanics of the 'two-handed' backhand (Figure 4).

![Fig. 4. Two phases of a tennis backhand: preparation and shot](image)
Naturally, all of this occurs in one fluid motion with precise timing so that maximum energy (and momentum) transfer occurs from loading to releasing. And, for maximum racket-head speed, some body segments may be slowed down to increase the speed of the racket, as in cracking a whip. Thus, we see that not only do we need some basic biomechanics at all levels of our tennis maturity, but as we advance in tennis, we even need a special biomechanics of whip-like movements, which is crucial to make every serve, forehand and backhand maximally efficient.

In particular, a topspin shot (Stepanek, 1988; Elliott et al., 1989a, 1989b) is hit by sliding the racquet up and over the ball as it is struck. By dragging the racquet over the ball, the friction between the racquet's strings and the ball is used to make the ball spin forward, towards the opponent. The shot dips down after impact and also bounces at an angle lower to the ground than a shot hit with no topspin. As a ball travels towards a player after bouncing, it has natural topspin that is caused by the friction of the tennis court. When hitting a topspin shot, the player is reversing the spin of the ball, which requires more energy.

On the other hand, a backspin shot is hit in the opposite manner, by sliding the racquet underneath the ball as it is struck. This causes the ball to spin towards the player who just hit it as it travels away. Generating slice, or backspin, requires only about half the racket head speed compared to hitting topspin, because the player is not required to change the direction in which the ball is spinning. The oncoming ball bounces off the court with topspin, spinning from top to bottom as it comes toward the player. When a player returns the ball with a slice shot the direction in which the ball spins around the axis of rotation is maintained. The direction of the shot changes, but the ball continues to spin from top to bottom, from the player's perspective as it moves away from the player.

2.2. Anatomical Description of Tennis Shots

2.2.1. The Serve

Instead of the fastest serve in the world, Andy Roddick's serve (which we will address later), we have chosen to analyze the standard serve (see Elliott et al., 1995), what happens to be Roger Federer's serve, which is also similar to Novak Đoković's serve. The following information explains the steps and muscles used to create this serve. Federer's serve has three stages: (i) the ball toss, (ii) the jump, and (iii) the finishing smash (see Figure 2).

The ball toss

In Federer's case, the ball toss is thrown with the left arm. The feet are apart, and the ball toss is performed with the contractions of the left deltoideus, the biceps and the palmar flexors muscles. This movement is done simultaneously with two other preparatory actions.

The first one of these preparatory actions is raising the right arm, "loading", part 1. The muscles used to carry this out are the right deltoideus, supraspinatus (a muscle going over the shoulder blade) and the biceps. The second action is bending the knees, and thus preparing for the second stage of the serve (the jump). There are no muscles used to bend the knees, not even the hamstring or knee-flexor muscles, for the bending of knees is accomplished by gravity alone.
The jump

Federer's serve jump is performed high and forward. It is achieved by instantaneous actions of all the leg extensor muscles; left and right soleus, quadriceps and gluteus maximus muscles. Jumping is the second part of "loading" in Federer's serve. At the same time as he lifts off, the racquet is placed behind the body, in a "back-scratching" position, and the right shoulder's rotation towards the ball begins. This movement involves the right biceps and wrist extensor muscles. While in the air, the feet naturally join together (with Federer, the feet join in the air, not on the ground).

The finishing smash

The finishing smash takes place in the air, before Federer returns to the ground. To end the serve, the shoulders are rotated and the ball is hit simultaneously. By then, the shoulders should have been fully rotated and the feet prepared for landing. The internal and external obliques abdominal muscles complete shoulder rotation. Hitting the ball is performed by the latissimus, then pectoralis major and finally triceps muscles. To add a bit of spin or slice to the serve, the wrist is flicked slightly at the end, using the palmar flexors.

2.2.2. The Forehand

We will analyse the standard forehand (see Elliott et al., 1997), what happens to be the forehand of Roger Federer, which is also similar to Novak Đoković's forehand. It basically has two phases: (i) preparation, or "loading", and (ii) hitting the ball.

Preparation, or "loading"

Preparation for the forehand includes two simultaneous actions. One is stepping into the right position, with the left leg forward (this applies for right-handers). The other is the first half of the "Sydney harbour" movement, lifting the racquet above the shoulders in a curved c-shaped movement. (This does not need to be too far back, like in Lleyton Hewitt's forehand, but can be more to the side.) This is accomplished by the right deltoideus and biceps muscles.

Hitting the ball

Hitting the ball includes four main movements. The first of these four is a right hip rotation towards the ball, while the feet are still on the ground. The right gluteus maximus and medius muscles carry out this action.

Secondly, a leap into the air is necessary to be able to hit the ball from a higher body position, so as not to hit the net. This is performed by all the leg extensor muscles; left and right soleus, quadriceps and gluteus maximus, working at the same time.

Thirdly, an arm swing of the racquet, the second part of the "Sydney harbour" action. The right pectoralis major, deltoideus and biceps muscles complete this.

Lastly, to create topspin; a slight twist of the wrist to just brush over the ball. This is done by the right palmar flexors.
2.2.3. The Backhand

We will next analyse one of the best double-handed backhands of tennis, Novak Đoković’s. Like the forehand, it basically has two stages: (i) preparation, or "loading", and (ii) hitting the ball.

Preparation, or "loading"

Preparation for the double-handed backhand includes two phases. One is stepping into the right position, with the right leg forward (this applies for right-handers). The other is lifting the racquet in a movement similar to the "Sydney harbour" of the forehand, only this time the racquet tends not to go further than about shoulder-level. This is accomplished by both the left and right deltoideus and biceps muscles.

Hitting the ball

Hitting the ball includes four main movements. The first of these four is a left hip rotation towards the ball. The left gluteus maximus and medius muscles carry out this action, helped by the left knee extension, which is performed by the quadriceps femoris.

Secondly, a rotation of the left shoulder towards the ball, is achieved by both the internal and external obliques abdominal muscles.

Thirdly, the arm swing of the racquet is performed by pulling of the right arm and pushing of the left arm. The pulling action of the right arm is accomplished by the right latissimus, pectoralis major and triceps muscles. The pushing action of the left arm is accomplished by the left deltoideus, pectoralis major and biceps muscles.

Lastly, to create topspin, a slight twist of both wrists is needed. This is done by the left palmar flexors and right dorsal flexors.

2.2.4. The Mystery of Roddick's Serve

A former world number one, and currently one of the top 10 ATP-ranked players, American Andy Roddick, holds the record for the world's fastest tennis serve: 153 m/h (or 246 km/h) fired at Queen's Club, UK, in 2004 (note that at the last Australian Open, Roddick fired the strongest serve of 237 km/h – and still lost the match). When he first met Patrick McEnroe, his Davis Cup coach, he said: "Whatever you do, don't say anything to me about my serve. If I think about it, I'm in trouble." Why? Because it is all subconscious, reflex movement, more precisely the stretch-reflex-based movement (see Houk, 1967, 1979; Ivančević, 2005, 2006). If you think about something that is performed reflexively, you simply mess it up. Therefore, it is crucial that the elite player develops a fully reflex-based technique that will generate the highest possible racket-head speed and thus maximize the athlete's performance / efficiency (assuming that they are already capable of consistently getting the serve into the square, keep their serve deep, able to serve to the opponent's backhand, body and/or forehand at will, and effectively use slice and/or topspin kick).

However, coaches and sports scientists should analyze the most efficient movements to be able to teach the model techniques. For example, Dr. Bruce Elliott from the University of Western Australia, has extrapolated the contributions of the body segments to racket-head speed (see Figure 5) using 3D video-and computer analysis. "These contri-
butions vary from person to person," Elliott says, "but the data shows the clear impor-
tance of the trunk, shoulder internal rotation and wrist flexion in the swing to impact."

Fig. 5. A snapshot of Andy Roddick's record serve (246 km/h), showing the contribution (in percentages) of the involved body segments and partial body movements.

2.3. Main Degrees-of-Freedom in Human Joints

All human movements take place in synovial rotational joints (Figure 6). Some joints are only slightly movable, formed by two bones held together by cartilage, without joint cavity (e.g., an intervertebral joint in the spine consists of two vertebrae and an intervertebral disc between them). On the other hand, major joints involved in human movement, like shoulder, hip, elbow and knee, are composed of several bones separated by a joint cavity, lubricated by synovial fluid and enclosed in a fibrous joint capsule (Marieb, 1998). Different joints have
different degrees-of-freedom (DOF) of movement: hinge joints have 1 DOF, gliding and saddle joints have 2 DOF, while ball-and-socket joints have 3 DOF.\footnote{1}

\footnote{1 Note that this is a simplified picture that is more valid for robot joints than for human joints. In reality, e.g., shoulder has 6 DOF, as well as hip and knee (the knee-cap travels about 7 cm from maximal flexion to maxima extension). If we take into account micro-translations that always follow the corresponding rotational movements in synovial joints, then the number of DOF is human joints is much higher, so an arm with a tennis racket represents a highly-redundant kinetic system.}

\textbf{Fig. 6. Main Degrees-of-Freedom in Human Joints}

\textbf{2.4. The Basic Biomechanical Unit}

Every human movement is driven by synergistic action of the basic biomechanical units. The basic biomechanical unit consists of a pair of mutually antagonistic muscles producing a common muscular torque, $T_{\text{Mus}}$, in the same joint, around the same axes. The most obvious example is the biceps-triceps pair (see Figure 7). Note that in the normal vertical position, the triceps downward action is supported by gravity, that is the torque due to the weight of the forearm and the hand (with the possible load in it).

An overview of main muscular groups used in tennis is given in Appendix.
2.5. Basic Dynamics of a Tennis Racket

Dynamics of a tennis ball motion (as well as a handball one) is governed by the
Newton-Euler's equations of motion or a rigid body in our 3D space. Obviously, this is
just a necessary approximation, because in reality, a ball is an elastic body, rather than a
rigid body.\(^2\) The efficiency of tennis shots (as well as handball throws) is determined by
the spatial trajectory and speed of the ball in all of its 6 degrees-of-freedom (DOF). This
spatial trajectory and speed of the ball (as well as the impact force) are exactly defined by
the six Newton-Euler's equations of motion of a tennis racket (or a throwing hand during
the handball throw).\(^3\)

A rigid body freely moving in space has 6 DOF: 3 translations (along the X,Y,Z-axes)
and 3 rotations (around the X,Y,Z-axes). (Ivančević, 2005, 2006). Newton's Causality
Principle states: a 3D-force is a cause of a 3D-linear acceleration, which is a cause of a
3D-linear velocity, which is a cause of a 3D-linear motion. Similarly, a 3D-torque is a
cause of a 3D-angular acceleration, which is a cause of a 3D-angular velocity, which is a
cause of a 3D-angular motion (see Figure 8).

Translational motion is in Figure 8 defined by 3 Newtonian equations of linear motion
of the type:

\[
\text{force (F)} = \text{mass (m)} \times \text{acceleration (a)}
\]

\(^2\) As the elastic-body dynamics, based on the tensor stress-strain relation, is much more complicated, we will
stick to our rigid-body approximation in this paper. Even true rigid-body dynamics is more complicated.

\(^3\) Basic dynamical difference between tennis shots and handball throws is in the tennis racket. In tennis, there is
a collision between the racket and the ball, mechanically determined by the conservation laws for both 3D linear
and angular momenta. This collision does not exist in handball, where the ball flies off directly from the hand (it
is carried through and then let go) during the throw. However, in the first approximation, we can neglect this
difference, by considering a racket to be just an additional link (effector) of the arm.
Similarly, rotational motion (labeled by superscript R) is in Figure 7 defined by 3 Eulerian equations of angular motion:

\[
\text{torque (T)} = \text{inertia-moment (I)} \times \text{rotational-acceleration (a^R)}
\]

Fig. 8. Spatio-temporal trajectory, velocity and acceleration of a tennis ball in all 6 DOF are defined by three Newton's equations of linear racket motion (formulae above the axes) and three (simplified) Euler's equations of angular racket motion (formulae below the axes).

\footnote{The three Euler equations of rotational ball motion are here simplified by neglecting the terms with the couple inertia moments of the tennis racket. In such a way simplified Eulerian rotational equations are completely symmetric to the Newtonian translational equations. A more thorough analysis would have these coupled inertial terms included. Mathematically, this realistic asymmetry is caused by the non-commutativity of the rotational SO(3)-group, that is, the order of rotations matters. On the other hand, the translation \( \mathbb{R}^3 \)-group is commutative, that is, the order of translations does not matter.}
The symbols in Figure 7 have the following specific meaning:

The dot over a variable denotes the derivative (rate of change) with respect to time; \( m \) is the racket mass;

- \( F_x, F_y, F_z \) – three components of the total translational force acting on the racket (including muscular force, gravity and air resistance) – along the \((X,Y,Z)\)-coordinate axes;
- \( a_x, a_y, a_z \) – three components of the total translational acceleration of the racket – along the coordinate axes;
- \( p_x, p_y, p_z \) – three components of the total translational momentum of the racket – along the coordinate axes;
- \( v_x, v_y, v_z \) – three components of the total translational velocity of the racket – along the coordinate axes;
- \( I_x, I_y, I_z \) – three inertia moments of the racket – around the \((X,Y,Z)\)-coordinate axes;
- \( a_{Rx}, a_{Ry}, a_{Rz} \) – three components of the total rotational (angular) acceleration of the racket – around the coordinate axes;
- \( p_{Rx}, p_{Ry}, p_{Rz} \) – three components of the total rotational (angular) momentum of the racket – around the coordinate axes;
- \( v_{Rx}, v_{Ry}, v_{Rz} \) – three components of the total rotational (angular) velocity of the racket – around the coordinate axes.

In biomechanics, the only active force is the muscular force that generates any human motion by coordinated action (synergy) of a number of basic biomechanical units (Figure 6). On the other hand, from the perspective of muscular-training physiology, the most important quality is power, which incorporates both strength and speed, mechanically defined as:

\[
\text{power (P)} = \text{force (F)} \times \text{velocity (v)}
\]

Physiologically, it corresponds to the area under the force-velocity curve (see Hill, 1938; Ivančević, 2005, 2006). Muscular power is the key element of all power-sports, including tennis and handball.

The future research along the proposed lines will have to include the following components:

- Estimation/calculation of all included inertial, elasticity and biomechanical parameters;
- Computer simulation based on numerical solution of the above Newton-Euler equations of the tennis racket motion, for various values of parameters, initial conditions and inputs (muscular forces), with the objective to determine the 3D translational and rotational trajectories, velocities and accelerations of the tennis (respectively, handball) ball; and
- Embedding the micro-electro-mechanical (MEMS) inertial sensors (a three-axial accelerometer and a three-axial gyroscope) into the frame of a tennis racket – this technology is still in the development phase.
2.6. Vestibular system: 3D-sensor for the general Newton-Euler dynamics of human motion

The general human motion also obeys the general Newton-Euler dynamics. This general Newton-Euler dynamics of human motion is continuously being tracked by neurodynamical sensors residing within the human head. The vestibular organ in the inner ear helps maintaining the head equilibrium by sending the brain information about the head motion, both linear/translational and angular/rotational.

The vestibular organs consist of three membranous semi-circular canals (SCC), and two large sacs, the utricle and saccule. All the vestibular organs share a common type of receptor cell, the hair cell. The SCC within the vestibular organ of each ear contains fluid and hair receptor cells encased inside a fragile membrane called the cupula. The cupula is located in a widened area of each canal called the ampulla. When you move your head, the fluid in the ampulla lags behind, pushing the cupula a very tiny bit that causes the hairs to also bend a very tiny bit. The bending hairs stimulate the hair cells, which in turn trigger sensory impulses in the vestibular nerve going to the brain to "report" the movement. Hair cells are amazingly sensitive. For example, a cupula movement of even a thousandth of an inch is detected by the brain as a big stimulus (see Molavi, 1997; Marieb, 1998; Enoka, 2001; Ivancevic, 2006).

The SCC are positioned roughly at right angles to one another in the three planes of space. Thus, the canals react separately and in combination to detect different types of angular head movement. They detect when we nod in an up and down motion (pitch), when we tilt our head to the side towards our shoulder (roll), and when we shake our head "no" in a side-to-side motion (yaw). The SCC are responsible for detecting any kind of rotational motion in the head, thus effectively sensing the Eulerian dynamics.

Two other vestibular organs are located in membranous sacs called the utricle and the saccule. On the inside walls of both the utricle and the saccule is a bed (a macula) of several thousand hair cells covered by small flat piles of calcium carbonate crystals which look like sand, imbedded in a gel-like substance. The crystals are called otoliths, a word which literally means "ear stones". In fact, the utricle and the saccule are often called the otolith organs.

When a person's head is in the normal erect position, the hair cells in the utricle lie approximately in a horizontal plane. When the head is tilted to one side, the stones want to slide "downhill". This moves the gel just enough to bend the sensory hairs. The bending hairs stimulate the hair cells, which in turn send a signal to the brain about the amount of head tilt. The stones also move if the person is accelerated forward and back, or side-to-side. Similarly, the hair cells in the saccule are oriented in somewhat of a vertical position when the head is erect. When a person tilts their head, or is accelerated up and down (as in an elevator), or moved forward and back, the otoliths move and a signal is sent to the brain. The signals from the otoliths in the saccule and the utricle complement each other and give us an integrated signal about our movement. The otolith organs are primarily responsible for detecting any degree of linear motion of the head, thus effectively sensing the Newtonian dynamics.
3. CONCLUSION

In this paper the basic biomechanics of tennis shots has been presented together with their analogy with handball throws. The main difference between these two ball games is in the tennis racket (with its own inertial and elastic characteristics). The importance of the present study is in presenting, for the first time in Serbian tennis literature, the basic tennis biomechanics and its analogy with the handball throws.

REFERENCES

5. Appendix – MindMap of the basic muscle groups
Cilj ovog rada je prikaz savremene teniske nauke širokoj naučnoj javnosti. Prezentirana je biomehanička analiza udaraca u tenisu i odgovarajuća dinamika reketa i lopte, zajedno sa analognim izbačajima u rukometu. Osnovna razlika između ove dve sportske igre je u teniskom reketu (kao dodatnom segmentu tela sa njegovim inercijalnim i elastičnim karakteristikama). Ovaj rad prezentuje anatomska, fiziološka i biomehanička analizu teniskog servisa, forhenda i bekhenda, kao i 3D Njutn-Ojlerovu dinamičku analizu kretanja tenskog reketa u toku ovih udaraca. U budućnosti, ovakva analiza ce morati da bude podržana numeričkim simulacijama, kao eksperimentalnim merenjem baziranim na inercijalnim senzorima (akcelerometrima i žiroskopima umetnutim u okvir teniskog reketa) za merenje brzina i ubrzanja i pokreta igrača u toku servisa, forhenda i bekhenda.

Ključne reči: udarci u tenisu, izbačaji u rukometu, biomehanička analiza, Njutn-Ojlerova dinamika, vestibularni i veštački senzori